

Seat No.:	Q. Paper Code: FTC-A-023		SET	P	
	Fabtech Technical Campus, College of Engineering & Research, Sangola				
	(An Autonomous Institute)				
	All UG Programs				
	Academic Year: -2025-26, Semester-I				
Engineering Mathematics-I (25UGS11004)					
Regular End Semester Examination 2025-26 [Dec./Jan.]					
Class:	F. Y. B. Tech.	Day & Date:	Saturday, 10/01/2026		
Duration:	03 Hrs.	Max. Marks:	60 Marks		
Time:	10:00 AM TO 01:00 PM				
Instructions:					
1) Q. No. 1 is compulsory. It should be solved in the first 30 minutes in the Page No.3 of answersheet.					
2) Don't forget to mention the question paper set (P/Q/R) on the top of the page 3.					
Q. 1	Multiple Choice Questions (MCQs) Each question carries 1 mark			Marks: 10	
				CO	BL
1	$(\sin \theta + i \cos \theta)^5 = \underline{\hspace{2cm}}$ a) $\sin 5\theta - i \cos 5\theta$ b) $\cos 5\theta - i \sin 5\theta$ c) $\cos 4\theta + i \sin 4\theta$ d) None			1	1
2	If $U = \cosh(x+iy)$ then imaginary part of U is _____ a) $\sinh x \sin y$ b) $-\sin x \cosh y$ c) $\sin x \cosh y$ d) $-\sinh(x) \sin y$			1	1
3	If $x = \sin(u + v)$ then $\frac{\partial x}{\partial v} = \underline{\hspace{2cm}}$ a) $\cos(u + v)$ b) $(u + v)$ c) $(u + v)$ d) $\sin(u + v)$			2	1
4	If $z = \tan^{-1}\left(\frac{x}{y}\right)$ then $\frac{\partial z}{\partial x} = \dots$ a) $\frac{x}{x^2+y^2}$ b) $-\frac{x}{x^2+y^2}$ c) $\frac{y}{x^2+y^2}$ d) $-\frac{y}{x^2+y^2}$			2	1
5	The function $f(x, y) = 0$ has a saddle point if----- a) $rt - s^2 > 0$ b) $rt - s^2 < 0$ c) $rt - s^2 = 0$ d) None			3	1
6	Let $u = f(x, y, z)$ be given function subject to $\phi(x, y, z) = 0$ then in Lagrange Method of undetermined multipliers, Lagrange function is given by $F(x, y, z, \lambda) = \underline{\hspace{2cm}}$ a) $f \cdot \lambda \phi$ b) $f/\lambda \phi$ c) $f\lambda + f \cdot \phi$ d) $f + \lambda \phi$			3	1
7	The order and degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^3 = \left(\frac{dy}{dx}\right)^{3/2}$ is _____ a) 2, 6 b) 6, 2 c) 2, 3 d) 3, 2			4	1
8	The orthogonal trajectories of the family of the circles $x^2 + y^2 = a^2$ where a is parameter are _____ a) $y = mx^2$ b) $y = mx$ c) $y^2 = mx^2$ d) none			4	1
9	If $\phi = 2x^3 + 3y^2 + 4z^2$ then $\text{curl}(\text{grad } \phi) = \underline{\hspace{2cm}}$ a) $\nabla^2 u$ b) ∇u c) 1 d) 0			5	1

10	Maximum value of directional derivative of scalar point function $\phi(x, y, z)$ is ____ a) $ \phi $ b) $ \nabla\phi $ c) $\nabla\phi$ d) None	5	1
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Q. No.	Questions			Marks	CO	BL
Q. 2	Attempt any two of the following			10		
1	If n is positive integer, then prove that: $(-1 + i\sqrt{3})^{3n} + (-1 - i\sqrt{3})^{3n} = 2^{3n+1}$			5	1	3
2	If $\tan(A + iB) = x + iy$, Prove that i) $\tan 2A = \frac{2x}{1-x^2-y^2}$ ii) $\tanh 2B = \frac{2y}{1+x^2+y^2}$			5	1	3
3	Prove that $\log(1 + e^{2i\theta}) = \log(2\cos\theta) + i\theta$.			5	1	3
Q. 3	Attempt any two of the following			10		
1	If $u = \log(1 + x^n + y^n)$, then find the value of $\frac{\partial^2 u}{\partial x \partial y} + \frac{\partial u}{\partial x} \cdot \frac{\partial u}{\partial y}$			5	2	3
2	If $u = \tan^{-1}\left(\frac{x^3 - y^3}{x + y}\right)$ then find the value of $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ and prove that $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = (1 - 4\sin^2 u) \sin 2u$			5	2	3
3	If $z = x^2 + y^2$, $x = \cos t$, $y = \sin t$, find $\frac{dz}{dt}$ at $t = \pi$.			5	2	3
Q. 4	Attempt any two of the following			10		
1	If $x = u(1 - v)$, $y = u \cdot v$ then Prove that, $J \cdot J' = 1$			5	3	3
2	Find the possible percentage error in computing parallel resistance 'r' of three resistances r_1, r_2, r_3 from the formula $\frac{1}{r} = \frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3}$, if r_1, r_2, r_3 are each in an error by 1%.			5	3	3
3	Find extreme values of $f(x, y) = x^3 + y^3 - 3axy$			5	3	3

Q. 5	Attempt any two of the following	10		
1	Solve: $(1 + x^2)dy = (e^{\tan^{-1}x} - y)dx$	5	4	3
2	Water at temperature $100^{\circ}C$ cools in 10 min to $88^{\circ}C$ in a room temperature $25^{\circ}C$. Find the temperature of water after 20 minutes.	5	4	3
3	When a switch is closed, the current built up in an electric circuit is given by $L\frac{di}{dt} + Ri = E$. If $L=640$, $R=250$, $E=500$, and $i=0$ when $t=0$, show the current will approach 2 amps, when $t \rightarrow \infty$.	5	4	3
Q. 6	Attempt any two of the following	10		
1	A particle moves along the curve $x = t^3 + 1$, $y = t^2$, $z = 2t + 3$ where t is the time. Find the components of its velocity and acceleration at $t=1$ in the direction of the vector $i + j + 3k$.	5	5	3
2	Prove that the vector $=(x+2y+az)i+(bx-3y-z)j+(4x+cy+2z)k$, solenoidal and determine the constant a, b, c if the vector is irrotational.	5	5	3
3	Find the directional derivative of $\phi = x^2y + y^2z + z^2x$ at $(2,2,2)$ in the direction of the normal to the surface $4x^2y + 2z^2 = 2$ at the point $(2,-1,3)$.	5	5	3

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1	Let $u = f(x, y, z)$ be given function subject to $\phi(x, y, z) = 0$ then in Lagrange Method of undetermined multipliers, Lagrange function is given by $F(x, y, z, \lambda) =$ _____				3	1
	(a) $f \cdot \lambda \phi$ (b) $f/\lambda \phi$ (c) $f\lambda + f \cdot \phi$ (d) $f + \lambda \phi$					
2	The order and degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^3 = \left(\frac{dy}{dx}\right)^{3/2}$ is _____				4	1
	(a) 2, 6 (b) 6, 2 (c) 2, 3 (d) 3, 2					
3	The orthogonal trajectories of the family of the circles $x^2 + y^2 = a^2$ where a is parameter are _____				4	1
	(a) $y = mx^2$ (b) $y = mx$ (c) $y^2 = mx^2$ (d) none					
4	If $\phi = 2x^3 + 3y^2 + 4z^2$ then $\text{curl}(\text{grad } \phi) =$ _____				5	1
	(a) $\nabla^2 u$ (b) ∇u (c) 1 (d) 0					
5	Maximum value of directional derivative of scalar point function $\phi(x, y, z)$ is ____				5	1
	a) $ \phi $ b) $ \nabla \phi $ c) $\nabla \phi$ d) None					
6	$(\sin \theta + i \cos \theta)^5 =$ _____				1	1
	a) $\sin 5\theta - i \cos 5\theta$ b) $\cos 5\theta - i \sin 5\theta$ c) $\cos 4\theta + i \sin 4\theta$ d) None					
7	If $U = \cosh(x+iy)$ then imaginary part of U is _____				1	1
	a) $\sinh x \sin y$ b) $-\sinh x \cos y$ c) $\sinh x \cos y$ d) $-\sinh(x) \sin y$					
8	If $x = \sin(u + v)$ then $\frac{\partial x}{\partial v} =$ _____				2	1
	a) $\cos(u + v)$ b) $(u + v)$ c) $(u + v)$ d) $\sin(u + v)$					
9	If $z = \tan^{-1}\left(\frac{x}{y}\right)$ then $\frac{\partial z}{\partial x} =$...				2	1
	a) $\frac{x}{x^2+y^2}$ b) $-\frac{x}{x^2+y^2}$ c) $\frac{y}{x^2+y^2}$ d) $-\frac{y}{x^2+y^2}$					

10	The function $f(x, y) = 0$ has a saddle point if----- a) $rt - s^2 > 0$ b) $rt - s^2 < 0$ c) $rt - s^2 = 0$ d) None	3	1
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1	If $u = \log(1 + x^n + y^n)$, then find the value of $\frac{\partial^2 u}{\partial x \partial y} + \frac{\partial u}{\partial x} \frac{\partial u}{\partial y}$			5	2	3
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3	If $z = x^2 + y^2$, $x = \cos t$, $y = \sin t$, find $\frac{dz}{dt}$ at $t = \pi$.			5	2	3
Q. 4	Attempt any two of the following			10		
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2	Prove that the vector $=(x+2y+az)i+(bx-3y-z)j+(4x+cy+2z)k$, solenoidal and determine the constant a, b, c if the vector is irrotational.	5	5	3
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2	If $\phi = 2x^3 + 3y^2 + 4z^2$ then $\text{curl}(\text{grad } \phi) =$ _____ a) $\nabla^2 u$ b) ∇u c) 1 d) 0				5	1
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10	The order and degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^3 = \left(\frac{dy}{dx}\right)^{3/2}$ is ____ a) 2, 6 b) 6, 2 c) 2, 3 d) 3, 2	4	1
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